# Object Partitioning Considered Harmful: Space Subdivision for BVHs 

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## Motivation

- Classical BVH construction is not perfect
- Looks only at primitive’s centroids

- How much more performance is there?


## Background

- SAH: $\operatorname{cost}(N)=C_{T}+\frac{S A\left(N_{L}\right)\left|N_{L}\right|+S A\left(N_{R}\right)\left|N_{R}\right|}{S A(N)}$
- Cost based BVH construction: Top-down
- Partition set of $N$ 's primitives into $N_{L}$ and $N_{R}$

- Take partition with minimal cost
- Exhaustive search: $O\left(2^{N}\right)$


## Classical BVH Construction



- Assumes finely tessellated geometry
- Primitive $\rightarrow$ point


## Can We Do Better?



- CBVH split
- Cost $\approx 700$

- Optimal partition
- Cost $\approx 100$


## Geometric Partitioning

- Regular approach: Partition N's primitives
- Evaluate $A A B B$ s, and use to compute cost
- $O\left(2^{N}\right)$ partitions to test
- Geometric partitioning:
- Fix child $A A B B$ s and put primitives according to SAH
- Some configurations are infeasible
- Child AABB boundaries इ boundaries of primitives
- $O\left(N^{12}\right)$ configurations to test


## Geometric Partitioning Example



- Boundaries of $N_{\text {Lor } R}$ incident with dotted lines
- $P_{4}$ shared $\rightarrow$ put into node with smaller SA


## Geometric Partitioning Example



- Configuration infeasible
- $P_{2}$ is not covered


## Practical Considerations

- $O\left(N^{12}\right)$ is actually $O\left(N^{6}\right)$
- Each side of the parent $A A B B$ is inherited by a child
- Select child $A A B B$ s on a regular grid
- Run-time: $O\left(G^{6} N^{0.5}\right)$ including cost calculation
- Choosing $G=R N^{1 / 6}$ yields $O\left(N^{1.5}\right)$
- Look at CBVH configurations as well



## Results: FPS Random Rays



- Classical BVH ■ Our Method (R=64) ■ Our Method (R=4K)



## Results: Surface Area Cost



- Classical BVH - Our Method (R=64) ■ Our Method (R=4K)



## Result Analysis

- Suspect: SAH
- Overlap + locally minimizing SAH has adverse effect
- Experiment: Use recursive cost evaluation
- Tree cost better than CBVH but slower FPS!
- Hypothesis: SA model needs space partitioning
- Intuition: Early ray termination
- New algorithm
- Penalize overlap in cost function
- Refine search space by allowing primitive splitting


## Splitting Primitives

- Feasible and infeasible configurations

- Two possible ways to split a primitive

- SAH cost is the same


## Search Spaces

- Child $A A B B \mathrm{~s} \in$ continuum inside parent's $A A B B$
- Not limited to boundary of primitives anymore
- Limit search to a grid for practical purposes
- Augment with search space of other algorithms
- CBVH \& KD-tree construction search spaces



## Penalizing Overlap

- Bias SAH to account for overlap

$$
\operatorname{cost}(N)=C_{T}+\left(1+C_{o} \frac{V\left(N_{L} \cap N_{R}\right)}{V(N)}\right) \frac{S A\left(N_{L}\right)\left|N_{L}\right|+S A\left(N_{R}\right)\left|N_{R}\right|}{S A(N)}
$$

- $C_{0}$ - the overlap penalty
- Standard SAH: $C_{O}=0$
- Standard SAH with space partitioning: $C_{O} \rightarrow \infty$


## The Generic Algorithm

- Parameters:
- Search space
- Overlap penalty
- Algorithm
- Take configuration $\in$ search space with lowest cost
- Interesting parameters
- CBVH: BVH, $C_{0}=0$
- Full: Grid + KD tree + BVH, $C_{O} \rightarrow \infty$
- KDBVH: KD tree, $C_{o}$ irrelevant


## Results: FPS Random Rays



- CBVH $\quad$ Full Search ■KDBVH



## Results: FPS Frustum Traversal



■CBVH - Full Search ■KDBVH


## Comparison to Pre-Splitting

-Sponza Rotated Sponza


## Role of Overlap Penalty

— Ray Cost — Size in MB


## Spatial Build Algorithm

- Implement KDBVH using sweep plane
- Extensions:
- Combine with CBVH to control size using $C_{o}$
- Sampling of cost function
- Issues: Might miss cost minimum
- Cost is quadratic between split plane positions



## Conclusion \& Future Work

- SAH inadequate without space partitioning!
- Generic framework to study BVH construction
- Can explore full $2^{N}$ search space
- Spatial build algorithm
- Fast with near optimal results
- Research early termination aware cost function


# Thank you! 

